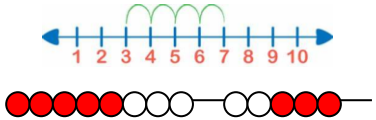
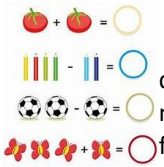
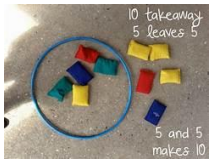
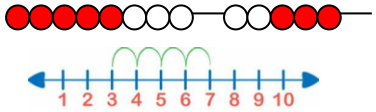
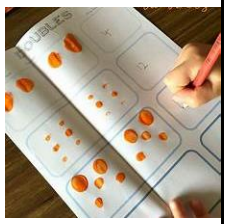
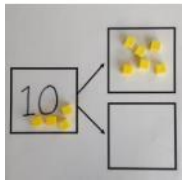
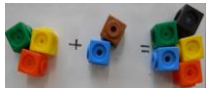
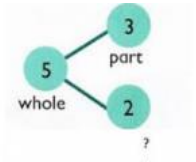
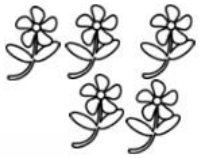
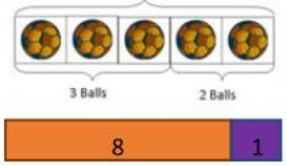
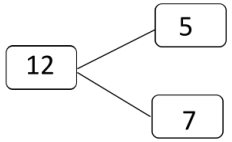
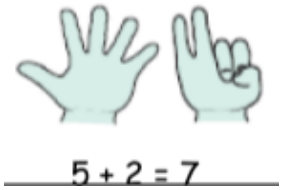
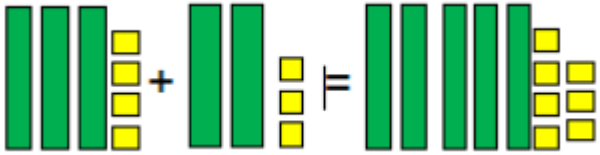
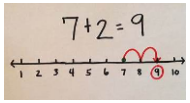
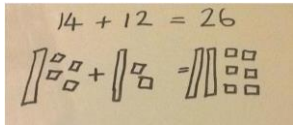
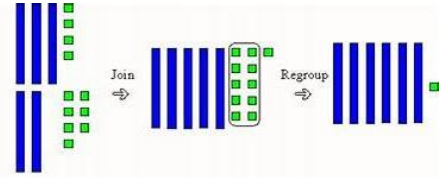
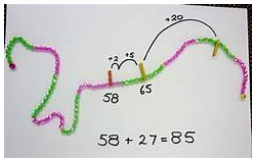
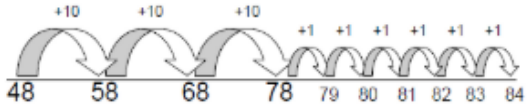
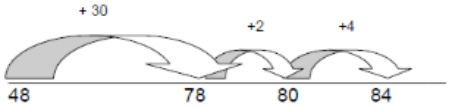
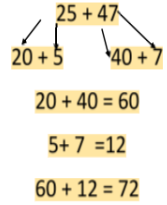
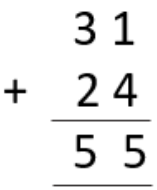
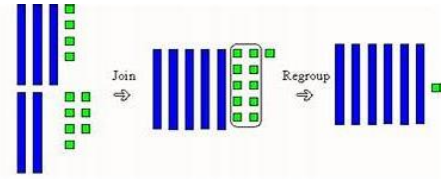
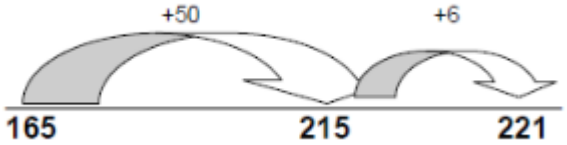
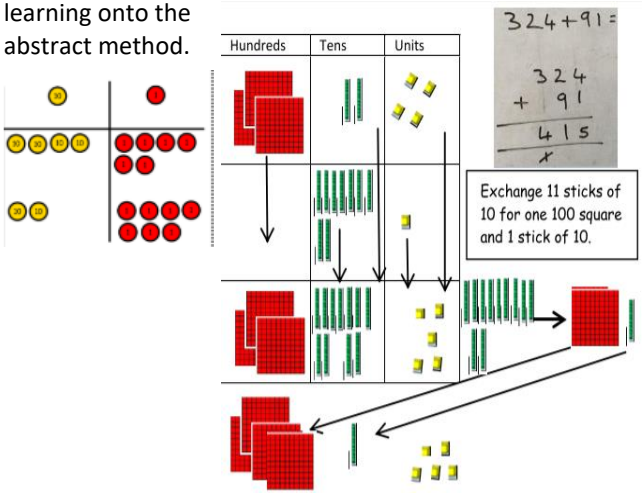
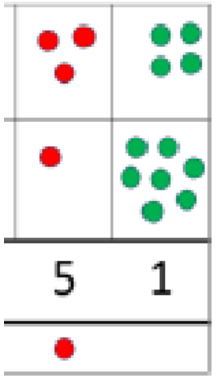
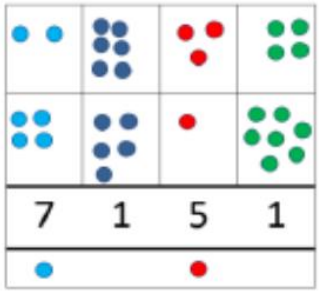
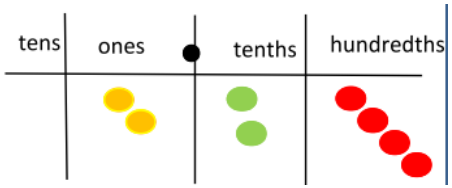
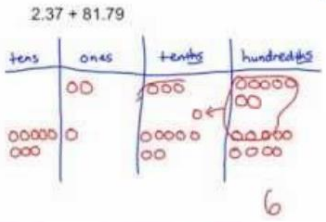
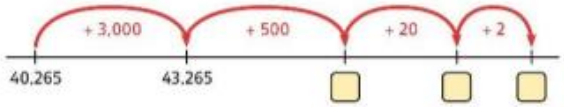
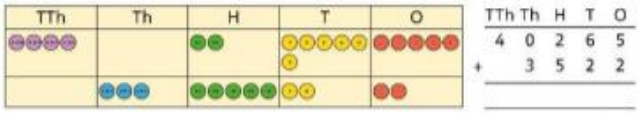
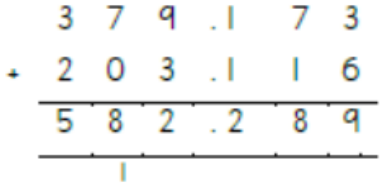
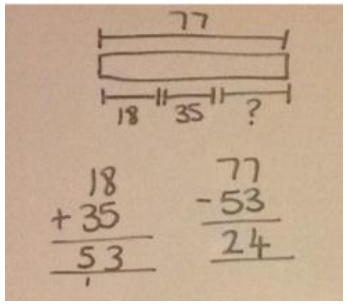
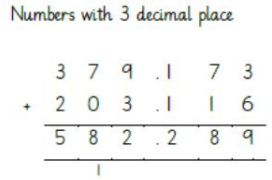
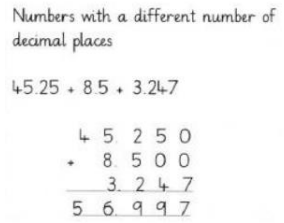
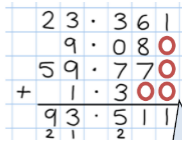
Calculation Policy January 2021

EYFS (Reception)			
Addition	**Subtraction**	**Multiplication**	**Division**
Children are encouraged to gain a sense of the number system through the use of counting concrete objects.  They combine objects in practical ways and count all.  They understand addition as counting on and will count on in ones and twos using objects, cubes, bead string and number line.  They use concrete and pictorial representation to record their calculations. They begin to use + and =  They are encouraged to develop a mental picture of the number system in their heads to use for calculations. Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.	Children are encouraged to gain a sense of the number system through the use of counting concrete objects.  They understand subtraction as counting out.  They begin to count back in ones and twos using objects, cubes, bead string and number line.  They use concrete and pictorial representation to record their calculations. They begin to use - and = They are encouraged to develop a mental picture of the number system in their heads to use for calculations. Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.	Children use concrete objects to make and count equal groups of objects.  They will count on in twos using a bead string and number line. They understand doubling as repeated addition. 2 + 2 = 4 They use concrete and pictorial representation to record their calculations.  Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.	Children use concrete objects to count and share equally into 2 groups. 6 cakes shared between 2 people each person gets 3 cakes. 6 ÷2 = 3  They count a set of objects and halve them by making two equal groups. They understand sharing and halving as dividing by 2. They will begin to use objects to make groups of 2 from a given amount. They use concrete and pictorial representation to record their calculations.  Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.

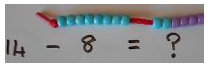
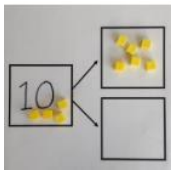
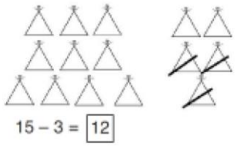
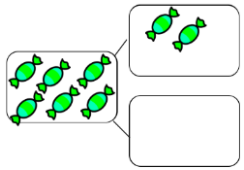
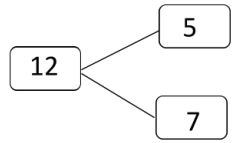
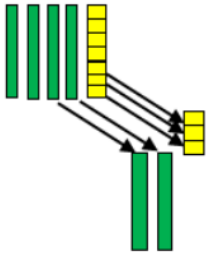
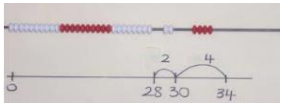
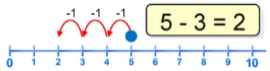
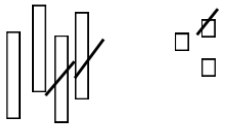
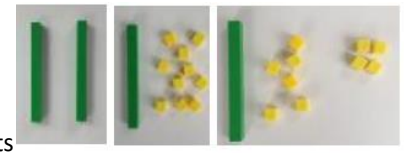
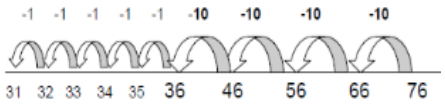
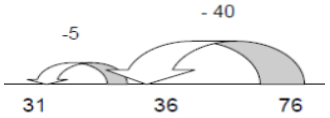
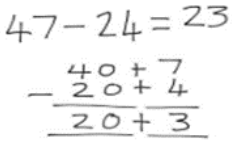
ADDITION - KS1 (Years 1&2)

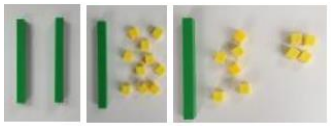
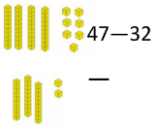
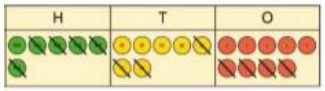
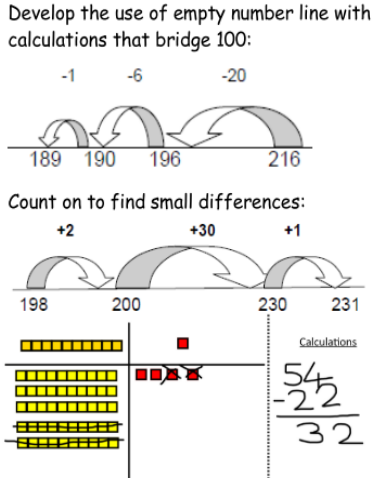
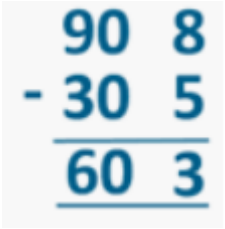
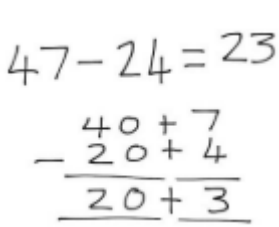
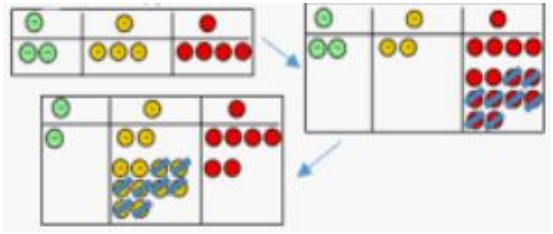
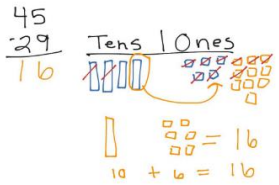
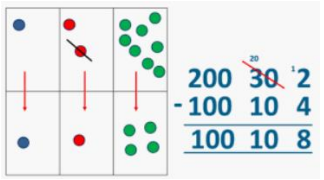
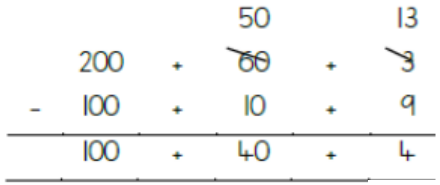
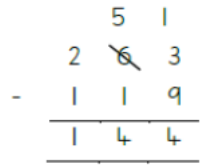
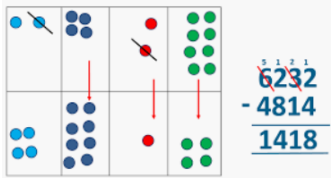
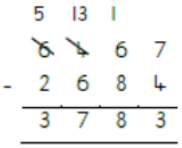
	Concrete	Pictorial	Abstract
Year 1	Use part/ part whole model, cubes and bead strings to add two numbers together as a group or in a bar.     	Use jottings to represent numbers.    Use pictures to add two numbers together as a group or in a bar.	Children will record their calculation using a pictorial method along with a calculation using numbers and symbols.  11 + 4 = 15 They may use their fingers to support their mental methods. 
Year 1 & 2	**Grouping objects to add** Children will use dienes cubes to add larger numbers where regrouping is not required. They will also use a bead string to add larger numbers by counting in tens and ones 	**Number line** Start at the larger number on the number line and count on in ones or in one jump to find the answer. Children will show their representations from the concrete method using pictures.   Numbers will get progressively larger throughout the keystage. Children will be able to add tens and ones using an empty number line.	Children will record their calculation using a pictorial method along with a calculation using numbers and symbols. 27 + 10 = 37 27 + 20 = 47 Children will begin to add multiples of tens. 27 + □ = 57
Year 2	**Partitioning** Children will add larger numbers where they will need to join, regroup and count.  Children will also use bead strings to add numbers together using groups of tens and ones to count on. 	**Number line** Use an empty number line to count in tens and then ones.  When confident: 	**Partitioning** Children will begin to use the partitioning method. Tens and ones will be added to form partial sums and then these partial sums will be added together to find the total.  Formal method: Finally an introduction to the column addition method. Focus on always starting with the smallest number in preparation for regrouping. 

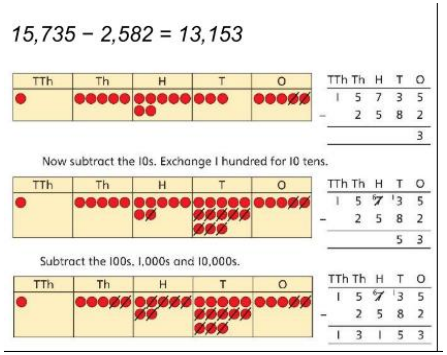
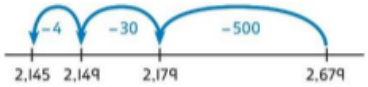
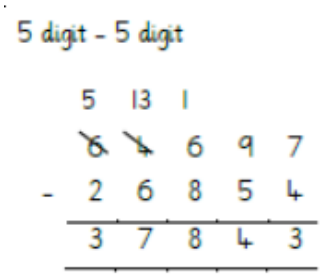
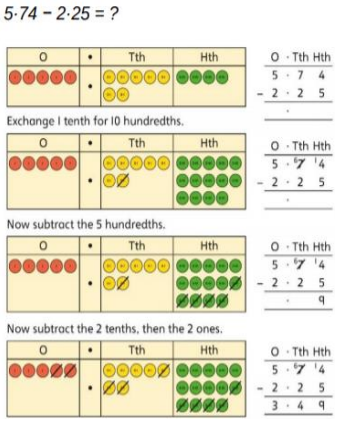
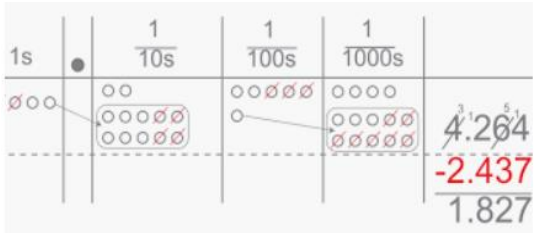
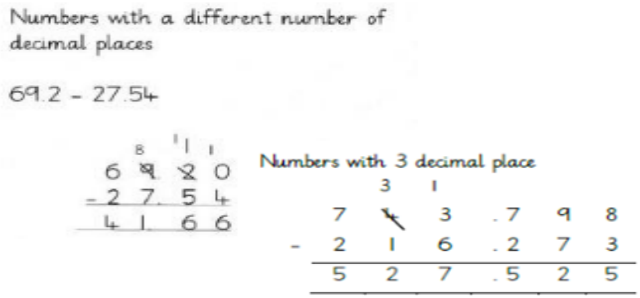
ADDITION - Lower KS2 (Years 3 & 4)			
	Concrete	**Pictorial**	**Abstract**
Year 3	Use dienes cubes to consolidate learning from KS1. Ensure children are confident at using these to join, regroup and count. This will support them moving onto the next stage of column addition. 	**Number line** Consolidate their learning from KS1 by using an empty number line to count larger numbers. 	**Partitioning** Children will consolidate using the partitioning method. The layout will begin to form a written method to support further progress onto the column method. Hundreds, Tens and ones will be added to form partial sums and then these partial sums will be added together to find the total. 200 + 60 + 3 + 100 + 10 + 9 300 + 70 + 12 300 + 80 + 2
Year 3	Introduce children to place value counters and dienes cubes. Use the column method layout to support their learning onto the abstract method. 	Children can draw a representation of the grid to further support their understanding, carrying the ten underneath the line. 	**Expanded column method - Formal method** Children to use the Expanded Column Method. Start by partitioning the numbers before the formal column to show the exchange. Once confident, they can move onto the column method in stage 3. 176 + 147 13 (7 + 6) 110 (70 + 40) 200 (100 + 100) 323 147 + 176 323
Year 4	Children will add larger numbers where they will need to exchange place value counters or dienes cubes. 	Children can draw a representation of the grid using larger numbers. 	**Column method – Formal method** Column Method for addition to be used. 4478 + 3762 8240 1 1 1

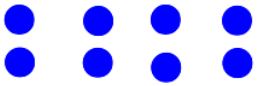
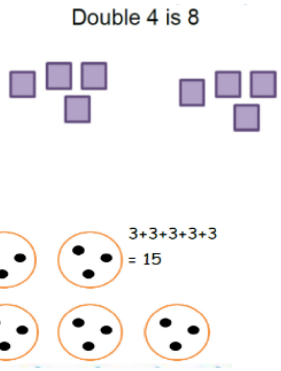
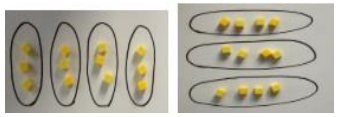
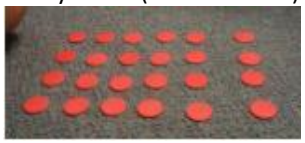
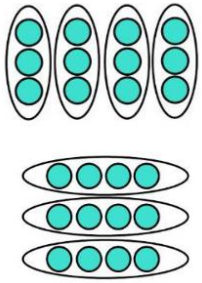
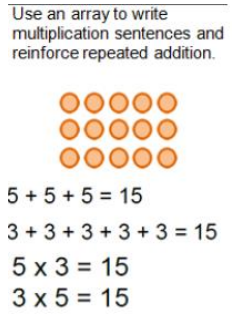
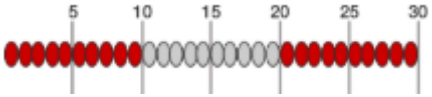
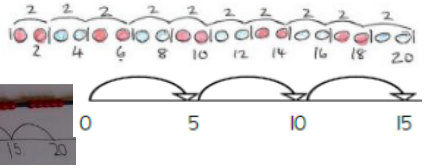
ADDITION - Upper KS2 (Years 5 & 6)			
	Concrete	**Pictorial**	**Abstract**
Year 5 & 6	Introduce decimal place value counters and model regrouping for addition.  Ten hundredths regroups to one tenth.	Children will draw their representations showing where they have regrouped.   	**Column method** Children will continue to develop their understanding of column method addition.  Calculations will become larger and include decimal places.
Year 5 & 6	Please note: Concrete apparatus and pictorial representations should still be used to support children who may be struggling with abstract concepts. Concrete apparatus should be readily available for lower achieving children and these with SEND.	Children will begin to use the bar model when problem solving. Jottings and calculations should be recorded to show their processes. 	**Column method** Children to further develop their confidence using the column method. Larger numbers, decimal places and inserting zero for place holders when decimals are different.    Insert zeros for place holders. 

SUBTRACTION - KS1 (Years 1&2)

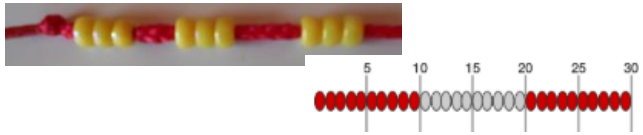
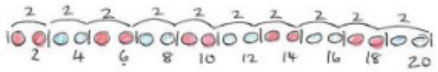
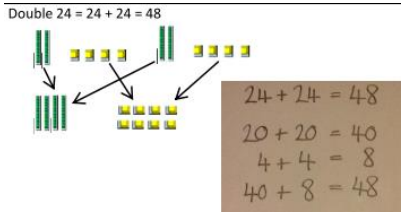
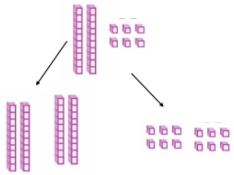
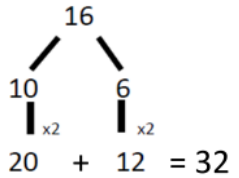
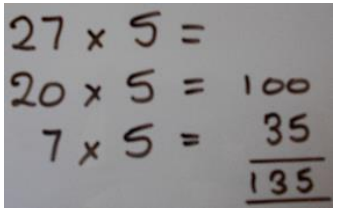
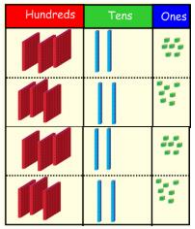
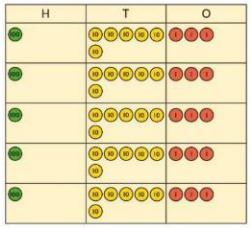
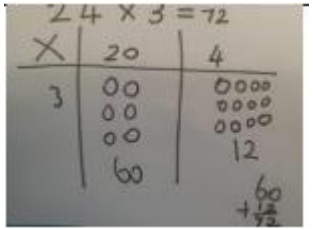
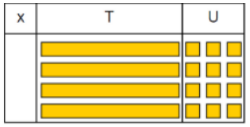
	Concrete	Pictorial	Abstract
Year 1	**Taking objects away** Use part whole model, cubes and bead strings to subtract two numbers together by moving objects away from the group.     	Use jottings to represent numbers. Children will learn to cross out drawn objects to show what has been taken away.  	Children will record their calculation using a pictorial method along with a calculation using numbers and symbols.  11 - 4 = 7 They may use their fingers to support their mental methods. 
Year 1 & 2	Children will use dienes cubes to subtract larger numbers where exchanging is not required. Children will lay out the first number using the dienes cubes and then move the second number away to show the subtraction.  They will also use a bead string to add larger numbers by counting in tens and ones.  	**Number line** Children will begin to draw their own number lines. Start at the larger number on the number line and count back in ones or in one jump to find the answer.  Numbers will get progressively larger throughout the key stage. Children will be able to subtract tens and ones using an empty number line. Children will show their representations from the concrete method using pictures.  43—21 = 22	Children will record their calculation using a pictorial method along with a calculation using numbers and symbols. 25 - 12 = 13 Children will begin to subtract multiples of tens. 25 - 10 25 - 10 = 15 15 - 2 = 13
Year 2	Children will begin to use place value counters and dienes cubes to show how to exchange between units of number. They will be able to change 1 ten and exchange it for 10 ones. 	**Empty number line -**Use an empty number line to count back in tens and then ones.  When confident:  	**Partitioning method** Children will begin to use the partitioning method. Tens and ones will be subtracted to form partial sums and then these partial sums will be added together to find the total.  47 – 23 = 24 47 – 20 = 27 27 – 3 = 24

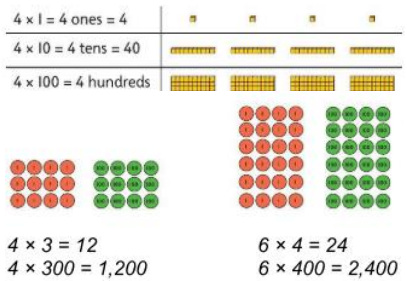
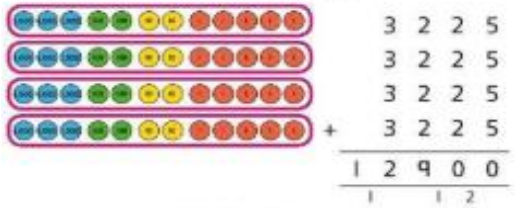
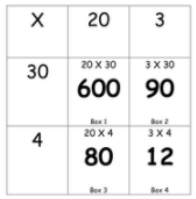
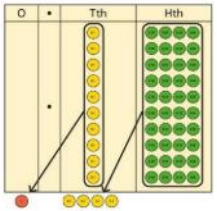
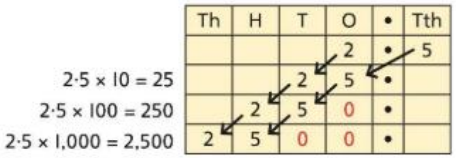
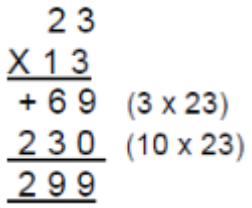
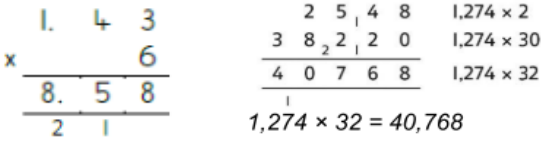
SUBTRACTION - Lower KS2 (Years 3 & 4)			
	Concrete	**Pictorial**	**Abstract**
Year 3	Children consolidate and use place value counters and dienes cubes to show how to exchange between units of number. They will be able to change 1 ten and exchange it for 10 ones.  They will be able to begin to lay this out like the column method and removing counters or cubes away to represent taking away.  	Consolidate their learning from KS1 by using an empty number line to calculate larger numbers. Children will also be able to draw representations of dienes cubes and place value counters by crossing out the number being taken away. 	  Children to further secure their knowledge using the **partitioning method** but will start to lay their work out using the column method approach. Tens and ones will be subtracted to form partial sums and then these partial sums will be added together to find the total.
Year 3	Children begin to set out HT0 - HTO using dienes cubes and place value counters (that cross the tens boundary) in columns and record as column subtraction with decomposition. Teach children how to exchange numbers. 	Children may draw dienes cubes or place value counters and cross off showing their understanding of taking away. They will need to represent any exchanging that takes place.  	**Partitioning method - with exchanging** Children will use the partitioning method to show exchanging.  Once confident, children can start to use the column method. 
Year 4	Children continue to develop their confidence in using dienes cubes and place value counters to show decomposition using the column method. 	Children draw representations from concrete activities using dienes cubes and place value counters. 	**Column Method** Children continue to use column method to subtract larger numbers. 

SUBTRACTION - Upper KS2 (Years 5 & 6)			
	Concrete	**Pictorial**	**Abstract**
Year 5 & 6	Please note: Concrete apparatus and pictorial representations should still be used to support children who may be struggling with abstract concepts. Concrete apparatus should be readily available for lower achieving children and these with SEND.	Children can draw using place value counters showing how exchanging takes place between the units of numbers.  Children also show subtraction on an empty number line using larger numbers. 	**Column Method** Children will continue to develop their understanding of column method subtraction.  Calculations will become larger.
Year 5 & 6	Introduce decimal place value counters and model exchange for subtracting between units of numbers. 	Children will draw their representations showing where they have exchanged. 	Calculations will become larger, include decimal places and require 0 to be added as a placeholder. 

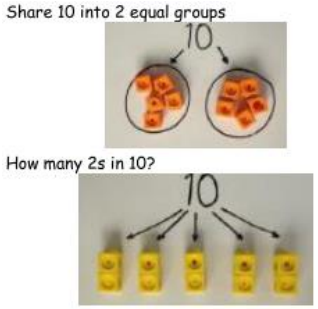
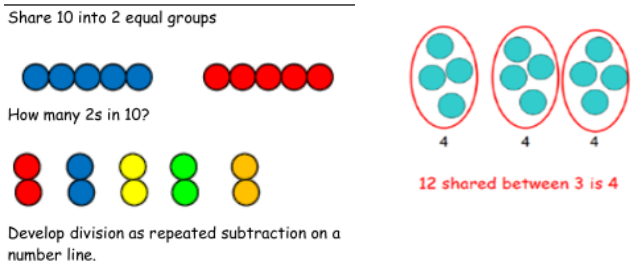
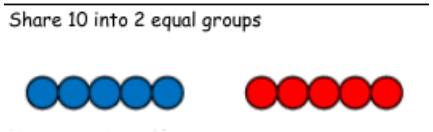
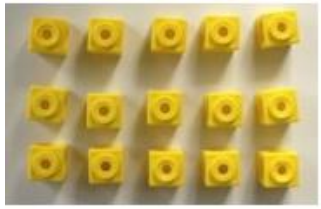
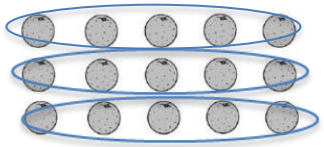
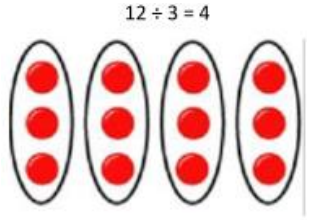
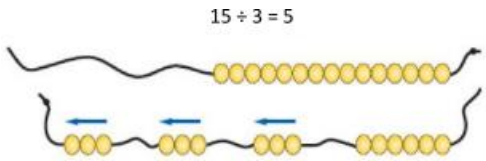
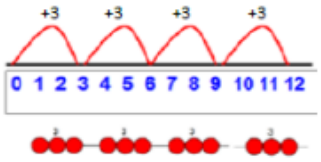
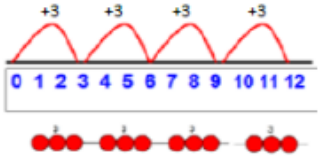
MULTIPLICATION - KS1 (Years 1&2)			
	Concrete	**Pictorial**	**Abstract**
Year 1	**Repeated addition - Groups of multiple objects** Children will count groups of the same number of objects and add them together. The children learn about grouping in practical contexts and through pictorial representations. 	Children draw representations to show counting in multiples and groups.  	Children show multiplication as repeated addition. Children may provide pictorial representations to support. 3 + 3 + 3 = 9 is the same as three lots of 3 or 3 x 3 = 9
Year 1 & 2	**Arrays** Children will be able to represent a multiplication calculation using an array and write the multiplication symbol within a number sentence. Children will also understand that multiplication can be carried out in any order (commutative).   	Children draw representations to show arrays. 	Children use arrays to show how to solve multiplication calculations. Children are able to show that multiplication can be done in any order (commutative). 3 x 5 = 15 5 x 3 = 15 Introduce x sign and record as number sentence 7 x 10 = 70 4 x 5 = 20 
Year 2	**Number line** Children will understand the operation of multiplication as repeated addition on a blank number line and will use practical resources to support this. Count the groups as children are skip counting, children may use their fingers as they are skip counting.  	Children will be able to use an empty number line to show multiplication as repeated addition. The use of beadsting concrete resources may be used to support conceptual understanding. 	Children show multiplication as repeated addition. 5 + 5 + 5 = 15 Introduce x sign and record as number sentence 7 x 10 = 70 4 x 5 = 20

MULTIPLICATION - Lower KS2 (Years 3 & 4)

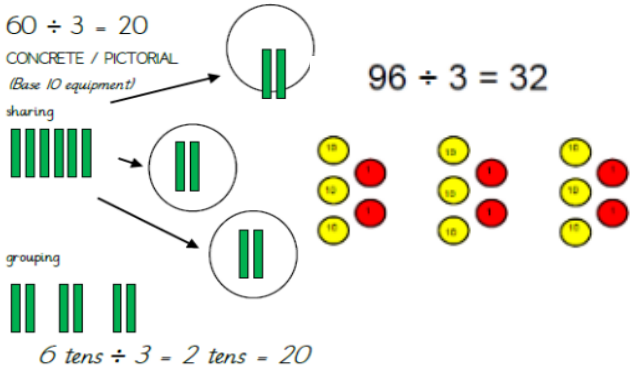
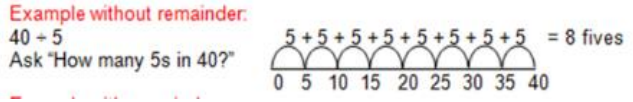
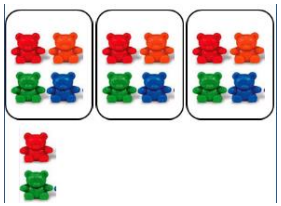
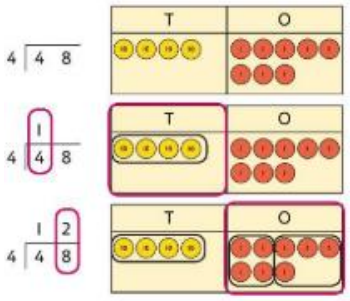
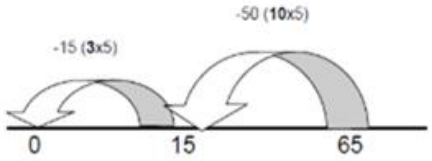
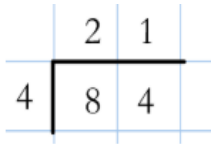
	Concrete	Pictorial	Abstract
Year 3	**Number line - Consolidation** Children will understand the operation of multiplication as repeated addition on a blank number line and will use practical resources to support this. Count the groups as children are skip counting, children may use their fingers as they are skip counting. 	Children will be able to use an empty number line to show multiplication as repeated addition. The use of beadsting concrete resources may be used to support conceptual understanding.   	Children show multiplication as repeated addition. 5 + 5 + 5 = 15 Introduce x sign and record as number sentence 7 x 10 = 70 4 x 5 = 20
Year 3 & 4	**Partitioning** Children will learn to multiply ones and tens separately before recombining the numbers back together. They can use Dienes cube of place value counters to achieve this. 	Children can draw representations of the partitioning process to support their conceptual understanding.  40 + 12 = 52	Partition a number and then multiply each part before recombining it back together. 16 x 2 =  
Year 3 & 4	**Grid Method** Show the links with arrays/ repeated addition to first introduce the grid method.  Move onto Dienes cubes to move towards a more compact method. Move on to place value counters to show how we are finding groups of a number. We are multiplying by 5 so we need 5 rows of that number. 	Pictorial representations can be made using their concrete manipulatives as visuals. They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown.   13 x 4 = (10 x 4) + (3 x 4) = 40 + 12 = 52	Children should be able to draw the grid method for each multiplication. The grid method will be used to show how this relates to a formal written method. **Grid method** X 30 6 4 120 24 Grid method will then lead to an introduction the formal method. Leading to expanded method 36 x 4 24 (6 x 4) 120 (30 x 4) 144 → 36 x 4 144 2

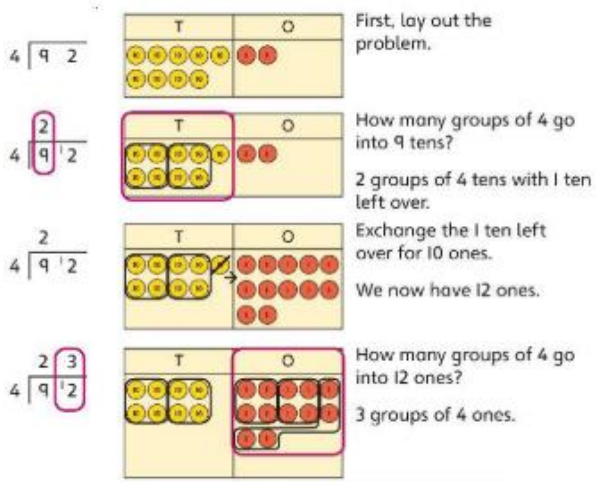
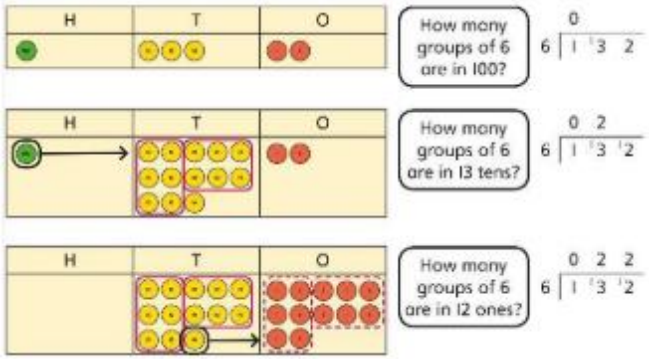
MULTIPLICATION - Upper KS2 (Years 5 & 6)			
	Concrete	**Pictorial**	**Abstract**
Year 5	Concrete materials (place value counters and dienes) may be needed to support children's conceptual understanding. When multiplying by 10, 100, 1000 initially concrete resources will be used to support understanding. Use place value equipment to multiply by 10, 100 and 1,000 by unitising.  4 × 3 = 12 4 × 300 = 1,200 6 × 4 = 24 6 × 400 = 2,400	Use place value equipment to compare methods. **Method 1**  3 2 2 5 3 2 2 5 3 2 2 5 + 3 2 2 5 1 2 9 0 0 1 1 2 **Method 2**  4 × 3,000 4 × 200 4 × 20 4 × 5 12,000 + 800 + 80 + 20 = 12,900	The **grid method** may be used to show how this relates to a formal written method. Grid method will lead onto **expanded method** and then onto the **compact short multiplication.** Example Question: 23 X 34  Use known facts and unitising to multiply. 5 × 4 = 20 5 × 40 = 200 5 × 400 = 2,000 5 × 4,000 − 20,000 5,000 × 4 = 20,000
Year 5 & 6	When multiplying decimals by 10,100,1000 initially concrete resources will be used to support understanding to show how exchanging can take place.  0·14 × 10 = 1·4	This pictorial grid method will support children's understanding of multiplying by 10, 100, 1000. 	**Long multiplication** Children may wish to use 2 separate calculations to support their understanding. Reinforce language of place value when multiplying by multiples of 10. Extend to 3 or 4-digit numbers multiplied by a 2-digit number. 
Year 6	Please note: Concrete apparatus and pictorial representations should still be used to support children who may be struggling with abstract concepts. Concrete apparatus should be readily available for lower achieving children and these with SEND.	Please note: Concrete apparatus and pictorial representations should still be used to support children who may be struggling with abstract concepts. Concrete apparatus should be readily available for lower achieving children and these with SEND.	Use column multiplication, ensuring understanding of place value at each stage.  1,274 × 32 = 40,768

DIVISION - KS1 (Years 1&2)

	Concrete	Pictorial	Abstract
Year 1	**Sharing and Grouping** Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding. 	Use pictures to share objects. Use circles rather than dots to aid counting. 	Children will be able to represent a division calculation using a pictorial method and write the division within a number sentence. $10 \div 2 = 5$ 
Year 1 & 2	**Arrays** Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg: 15 ÷ 3 = 5 5 x 3 = 15 15 ÷ 5 = 3 3 x 5 = 15 	Draw arrays to show how pictures are divided. 15 ÷ 3 = 5 or 15 ÷ 5 = 3 	Children will be able to represent a division calculation using an array and write the division within a number sentence. 
Year 2	Repeated addition and subtraction through making 'groups of…' Children will understand the operation and repeated addition or subtraction using bead strings and number lines. This will support the pictorial element. 	Children will understand the operation of division as grouping using repeated addition or subtraction on a prepared number line.  **12 ÷ 3 = 4**	Children will be able to represent a division calculation using a number line and write the division within a number sentence. This can be further developed to counting on using times tables. 20 ÷ 5 = 5 10 120  **12 ÷ 3 = 4** (Year 2 focus times tables 2, 5, 10 only)

DIVISION - Lower KS2 (Years 3 & 4)

	Concrete	Pictorial	Abstract
Year 3	**Division with no remainders through sharing**. Use concrete materials to share into groups. 	Consolidate learning from KS1 using diagrams of sharing and repeated subtraction and addition on a number line to make jumps  Concrete methods could be represented pictorially within books to show understanding.	How many groups of 6 in 24? $24 \div 6 = 4$ Abstract methods may be supported with pictorial methods within the children's books. This can be further developed to counting on using times tables. 6 12 18 24 (Year 3 focus times tables 2, 5, 10, 3, 4, 8)
Year 3 & 4	**Division with remainder through sharing** 14 ÷ 3 = Divide objects between groups and see how much is left over/ remaining.  **Division no remainders - introduction to bus stop method** Use place value equipment on a place value grid alongside short division. The model uses grouping. 'How many groups of…can you make?' 	Students can continue to use drawn diagrams with circles to help them divide numbers into equal groups. Remainders will be seen by not fitting into a whole group. Draw dots and group them to divide an amount and clearly show a remainder.  Continue to use blank number lines as appropriate, using multiples of the divisor. 65 ÷ 5 = 13 	Children will begin to move onto division with remainders. A number sentence will support any abstract written calculation by using pictorial method to support.  **Short division** Children will begin to use the formal written method of division without remainders. This will only come after a clear concept is understood using manipulatives.  Dividing by 2,3,4, and 5

Year 4	**Division with remainders - Bus stop** 	Pictorial representations can be used to support any concrete manipulatives. 	**Chunking** Chunking is repeated subtraction of the divisor and multiples of the divisor. **Bus Stop** 73 ÷ 5 5 | 73 - 50 (10 x 5) 23 - 20 (4 x 5) 3 10 + 4 = 14 **How many 5s have been subtracted?** **14 sets of 5, with 3 left over.** Answer: 73 ÷ 5 = 14 r3 **Method for division** 2 1 8 (3) 4 | 8 7 2 Move onto divisions with a remainder. 8 6 r 2 (3) 5 | 4 3 2

	DIVISION - Upper KS2 (Years 5 & 6)		
	Concrete	**Pictorial**	**Abstract**

Year 5

Dividing whole numbers by 10, 100 and 1,000

Use place value equipment to support unitising for division.

4,000 ÷ 1,000



4,000 is 4 thousands.

4 × 1,000= 4,000

So, 4,000 ÷ 1,000 = 4

Concrete and pictorial representations may still be required to support the formal method of division (Bus Stop) - Go back to LKS2 to consolidate learning.

Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.

Th	H	T	O
3	2	0	0

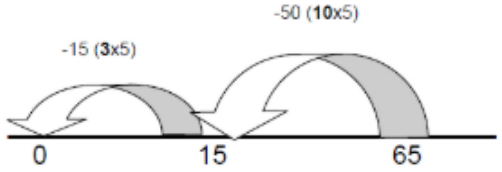
3,200 ÷ 100 = ?

3,200 is 3 thousands and 2 hundreds.
200 ÷ 100 = 2
3,000 ÷ 100 = 30
3,200 ÷ 100 = 32

So, the digits will move two places to the right.

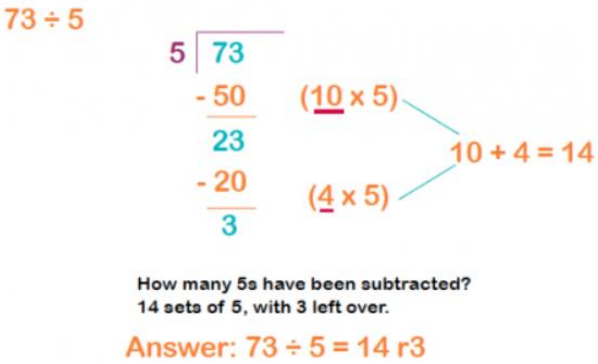
Continue to use blank number lines as appropriate, using multiples of the divisor.

65 ÷ 5 = 13

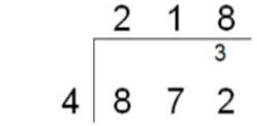


Chunking

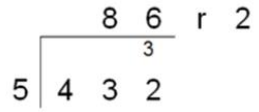
Chunking is repeated subtraction of the divisor and multiples of the divisor.



Bus Stop Method for division



Move onto divisions with a remainder.

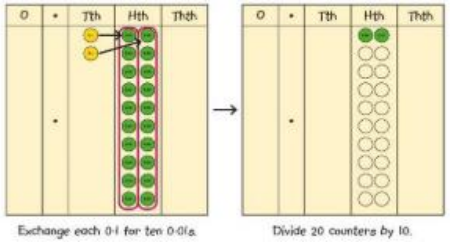


Year 5 & 6

Dividing decimals by 10, 100 and 1,000

Use place value counters to represent dividing by 10, 100, 1000. Represent division using exchange on a place value grid.

0·2 is 2 tenths.
2 tenths is equivalent to 20 hundredths.
20 hundredths divided by 10 is 2 hundredths.



Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid.

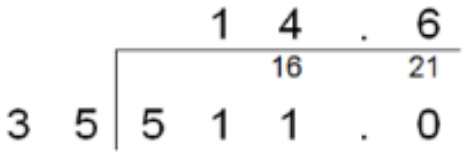
O	•	Tth	Hth	Thth
0	•	8	5	
0	•	0	8	5

0·85 ÷ 10 = 0·085

O	•	Tth	Hth	Thth
8	•	5		
0	•	0	8	5

8·5 ÷ 100 = 0·085

Finally, move into decimal places to divide the total accurately using a formal method for division (bus stop).



Year 6

Long Division - Abstract Method

Calculations will start with tens and ones and move onto more advanced division calculations.

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o 2 2)5 8	t o 2 2)5 8 - 4 1	t o 2 9 2)5 8 - 4 ↓ 1 8
Two goes into 5 two times, or 5 tens ÷ 2 = 2 whole tens -- but there is a remainder!	To find it, multiply 2 × 2 = 4, write that 4 under the five, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.